

Willkommen zur Vorlesung  
*Sicherheit:*  
*Fragen und Lösungsansätze*  
im Wintersemester 2012 / 2013

Prof. Dr. Jan Jürjens

TU Dortmund, Fakultät Informatik, Lehrstuhl XIV

Teil 5 (Fundamentals of Cryptography)  
v. 03.12.2012



## Part I: Challenges and Basic Approaches

- 1) Interests, Requirements, Challenges, and Vulnerabilities
- 2) Key Ideas and Combined Techniques

## Part II: Control and Monitoring

- 3) Fundamentals of Control and Monitoring
- 4) Case Study: UNIX

## Part III: Cryptography

- 5) **Fundamentals of Cryptography**
- 6) Case Studies: PGP and Kerberos
- 7) Symmetric Encryption
- 8) Asymmetric Encryption and Digital Signatures with RSA
- 9) Some Further Cryptographic Protocols

## Part IV: Access Control

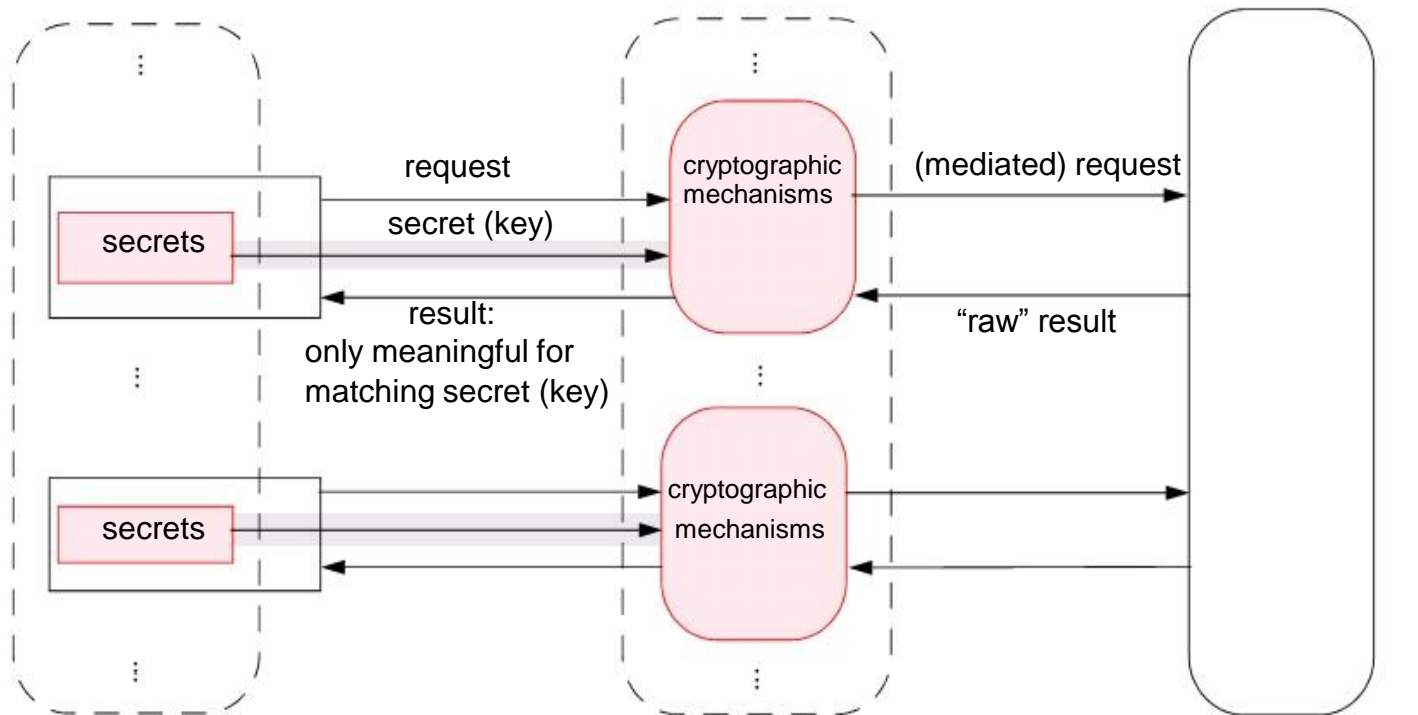
- 10) Discretionary Access Control and Privileges
- 11) Mandatory Access Control and Security Levels

## Part V: Security Architecture

- 12) Layered Design Including Certificates and Credentials
- 13) Intrusion Detection and Reaction

conceptually: (cryptographic)  
**knowledge base on permissions**  
(and prohibitions)

conceptually: (cryptographic)  
**control component**



**participating subjects**

- generate, store and employ secrets
- exploit physical isolation (indicated by the gray areas)

**controlled objects**



- is usually closely intertwined with control and monitoring
- binds a successful and meaningful execution of an operation or interaction to providing a suitable *secret key* as input
- achieves *virtual isolation* between participants: participants that share a cryptographic key are virtually isolated from those that do not
- enables *cooperation in the presence of threats* based on limited trust: participants that autonomously generate and secretly keep appropriate cryptographic keys can enforce their security *interests* by themselves

# Basic cryptographic blocks



- encryption
- authentication
- anonymization
- randomness and pseudorandomness
- one-way hash functions
- timestamps



- the sender  $S$  transforms the original bit string  $m$  to be transmitted into another bit string  $m'$ 
  - such that *only* the designated receiver  $R$  (and possibly the sender) is enabled to recover the original bit string
- (probabilistic) *key generation* algorithm  $Gen$  (one parameter and one result):
  - $l$  security parameter (key length, ... )
  - $(ek_R, dk_R)$  matching key pair
- (probabilistic) *encryption* algorithm  $Enc$  (two parameters and one result):
  - $ek_R$  encryption key
  - $m$  plaintext (original message)
  - $m' = Enc(ek_R, m)$  ciphertext (transformed bit string)
- (probabilistic) *decryption* algorithm  $Dec$  (two parameters and one result):
  - $dk_R$  decryption key
  - $c$  ciphertext
  - $c' = Dec(dk_R, c)$  (hopefully) recovered plaintext

# Encryption: correctness property



- encryption algorithm  $Enc$  and decryption algorithm  $Dec$  should be inverse whenever a *matching key pair*  $(ek_R, dk_R)$  generated by  $Gen$  has been employed:

for all plaintexts  $m$ ,  $Dec (dk_R, Enc (ek_R, m)) = m$



- ***naive version***  
for all plaintexts  $m$ , without a knowledge of the decryption key  $dk_R$ ,  
 $m$  cannot be “determined” from the ciphertext  $m$
- ***(informal) semantic version***  
an unauthorized observer of a ciphertext cannot infer  
anything new about the corresponding plaintext, i.e.,  
for all plaintexts  $m$ , without a knowledge of the decryption key  $dk_R$ ,  
any *property* of  $m$  that can be “determined” from the ciphertext  $m$   
could also be “determined” without knowing  $m$  at all
- ***(informal) operational version***  
an unauthorized observer of ciphertexts  
cannot separate apart any pair of ciphertexts, and thus  
cannot solve the problem of  
assigning a specific plaintext to a ciphertext



# Operational secrecy as indistinguishability



for a *probabilistic* setting, considering sequences of plaintexts and of matching key pairs of *increasing* length (taken as a *security parameter*), we have *indistinguishability of ciphertexts*:

for any pair of plaintext sequences

$(m_1', m_1'', m_1''', \dots)$

and

$(m_2', m_2'', m_2''', \dots),$

without a knowledge of the sequence of decryption keys employed, the resulting sequences of ciphertexts are “computationally indistinguishable”



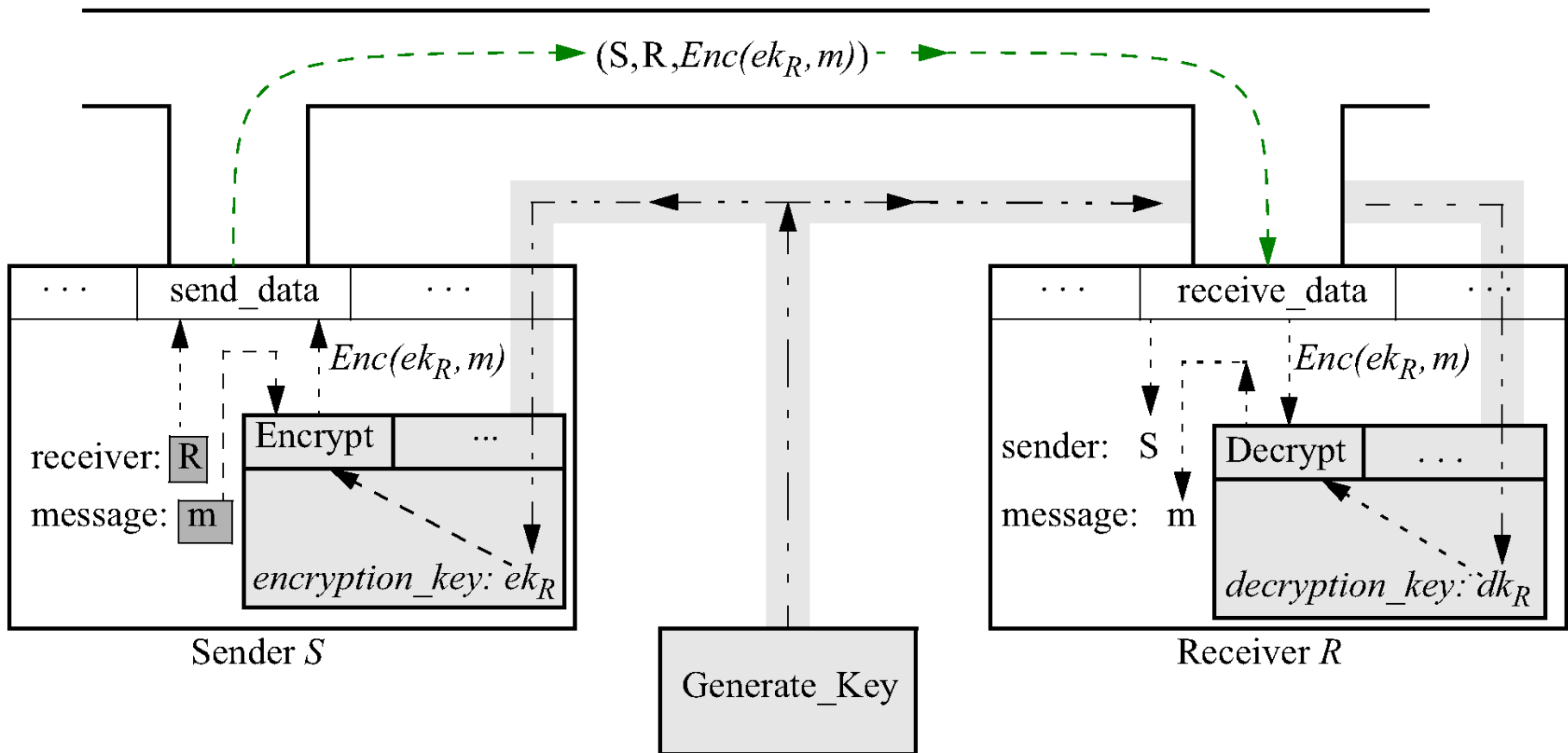
- approved algorithms *Gen* and *Dec* and *Enc* are publicly known
- decryption keys are strictly kept secret
- given approved algorithms and seen from the perspective of the end-users, enforcing the *confidentiality* of messages by encryption basically relies *only* on
  - selecting appropriate keys (as determined by the security parameter)
  - actually hiding the decryption keys

# Relationship between encryption key and decryption key

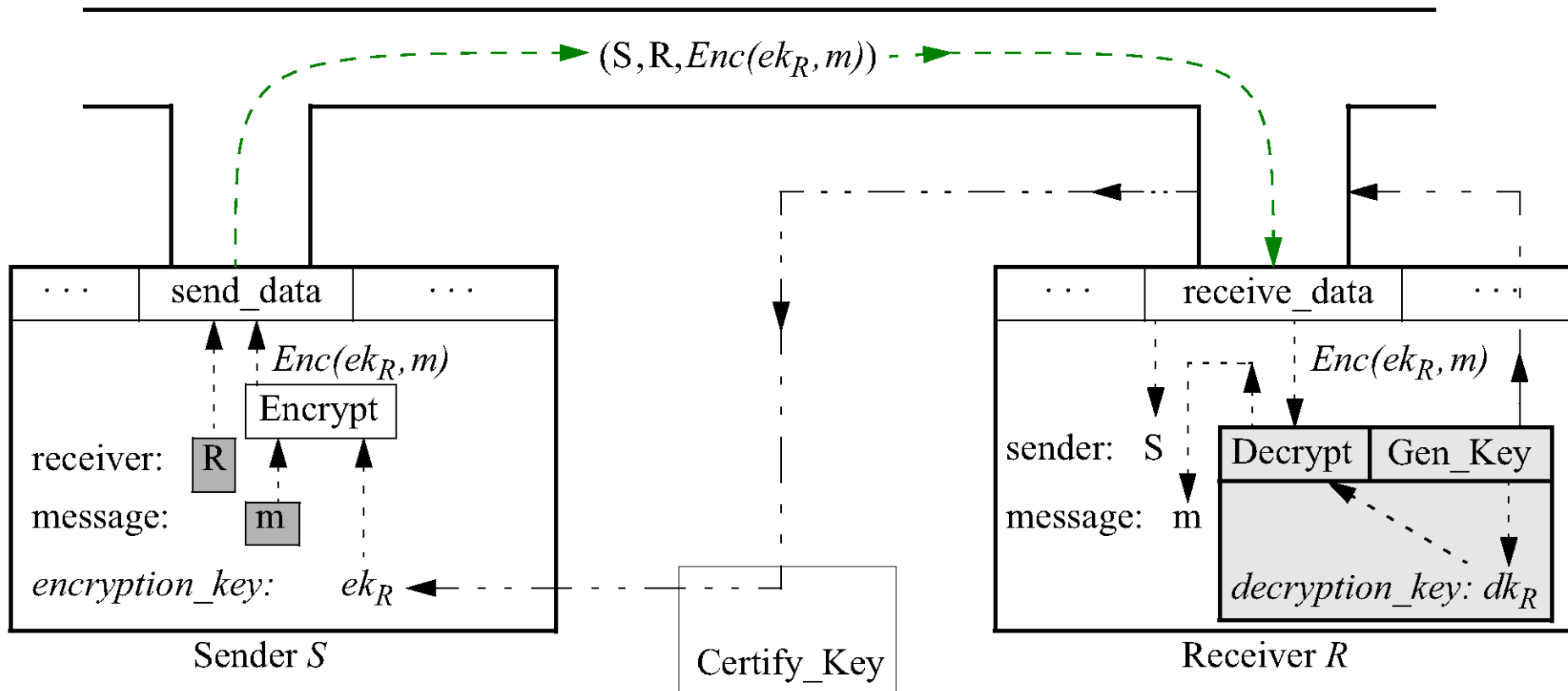


- **symmetric (or secret-key) mechanism:**
  - the encryption key is (basically) *equal* to the decryption key
- **asymmetric (or public-key) mechanism:**
  - the encryption key is essentially *different* from the decryption key
  - an additional *secrecy property* (*naive* version) is required:
    - the (private) decryption key  $dk_R$
    - cannot be “determined” from the (public) encryption key  $ek_R$

# Symmetric encryption



# Asymmetric encryption



# Symmetric and asymmetric encryption mechanisms

Feature	Symmetric	Asymmetric
<i>generating and distributing keys</i>	both partners are <i>equally</i> involved	designated <i>receiver</i> has a <i>distinguished</i> role
<i>protection requirements</i>	key generation / communication of the secret key and storage of the secret key must be protected on <i>both sides</i>	key generation and storage of the private key must be protected on the side of the <i>receiver only</i>
contributions of the <i>trusted third parties</i>	generate and distribute secret keys	certify public keys



## designated sender $S$

- prepares for transmitting a bit string  $m$  as a message by computing another bit string  $red_{S,m}$  as a *cryptographic piece of evidence* (*cryptographic exhibit* or *cryptographic check redundancy*)
- forwards the compound  $(S, m, red_{S,m})$ 
  - $S$  sender identification
  - $m$  original bit string
  - $red_{S,m}$  computed bit string

## receiver

- receives such a compound of the form  $(S, m, red_{S,m})$
- checks whether the message part originates from the claimed sender without modification by inspecting the included cryptographic exhibit (must depend on both the designated sender and the message)
- either accepts (as authentic) or rejects the received message

# Authentication: functionality

- (probabilistic) *key generation* algorithm *Gen* (one parameter and one result):
  - $l$  security parameter (key length, ... )
  - $(tk_S, ak_S)$  matching key pair
- (probabilistic) *authentication* algorithm *Aut* (two parameters and one result):
  - $ak_S$  authentication key
  - $m$  message
  - $red_{S,m} = Aut(ak_S, m)$  cryptographic exhibit
- (probabilistic) Boolean-valued *authenticity verification* algorithm *Test* (three parameters and Boolean result):
  - $tk_S$  test key/verification key
  - $m$  received message
  - $red$  cryptographic exhibit



# Authentication: (weak) correctness property



- authentication algorithm  $Aut$  and authenticity verification algorithm  $Test$  should be complementary whenever a *matching key pair*  $(tk_S, ak_S)$  generated by  $Gen$  has been employed:

for all messages  $m$ ,  $Test(tk_S, m, Aut(ak_S, m)) = true$



- **(naive) unforgeability property**  
for all messages  $m$ ,  
without a knowledge of the authentication key  $ak_S$ ,  
one cannot “determine” a bit string  $red$  such that  $Test(tk_S, m, red) = true$
- **(naive) strong correctness property,**  
complemented by a **weak unforgeability property**  
for all messages  $m$  and for all bit strings  $red$ ,  
 $Test(tk_S, m, red) = true$  iff  $red = Aut(ak_S, m)$   
and  
without a knowledge of the authentication key  $ak_S$ ,  
one cannot “determine” this solely accepted cryptographic exhibit



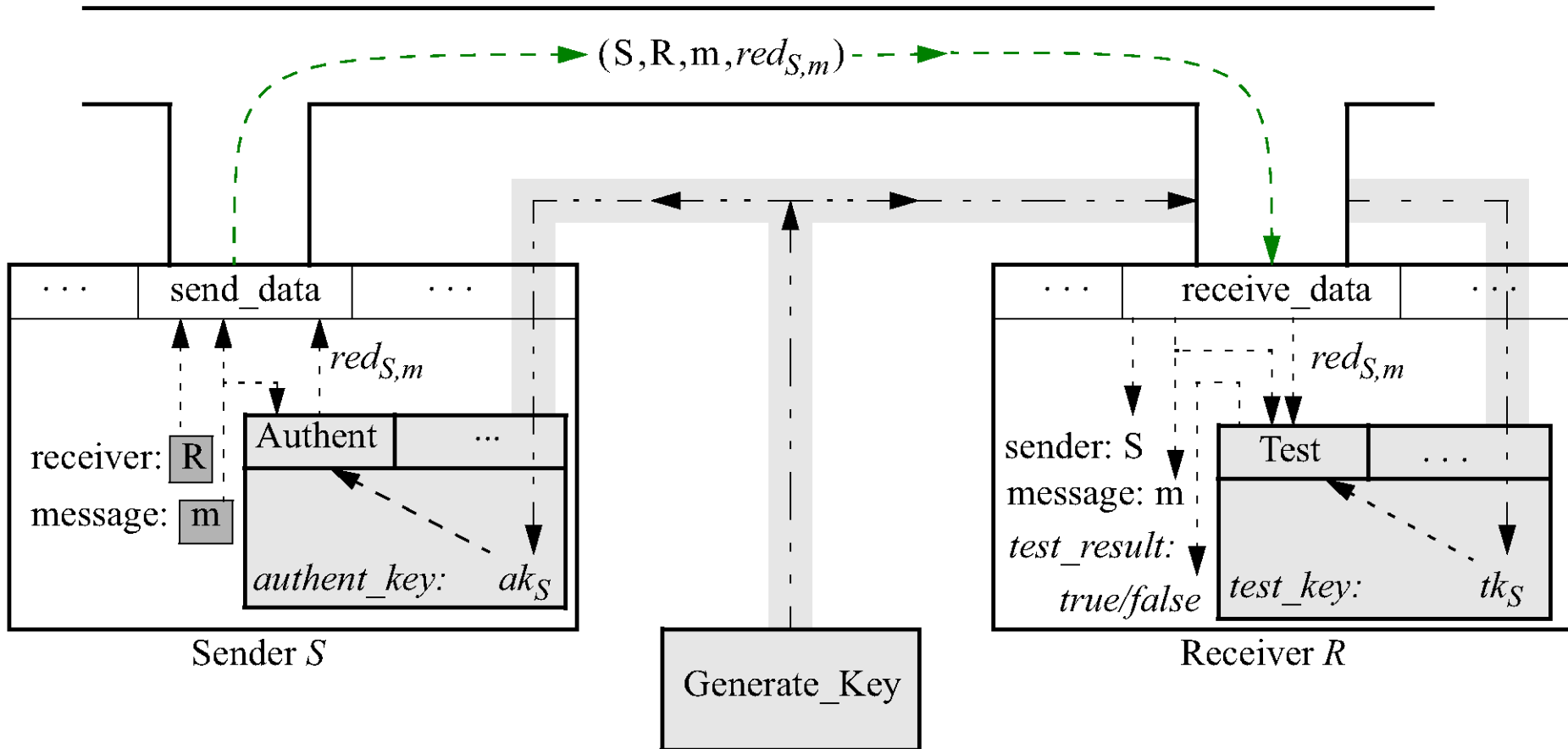
- approved algorithms *Gen*, *Aut* and *Test* are publicly known
- authentication keys are strictly kept secret
- given approved algorithms and seen from the perspective of the endusers, enforcing the *integrity* and *authenticity* of messages (in the sense of detection of violations) by authentication basically relies *only* on
  - selecting appropriate keys (as determined by the security parameter)
  - actually hiding the authentication keys

# Relationship between test key and authentication key

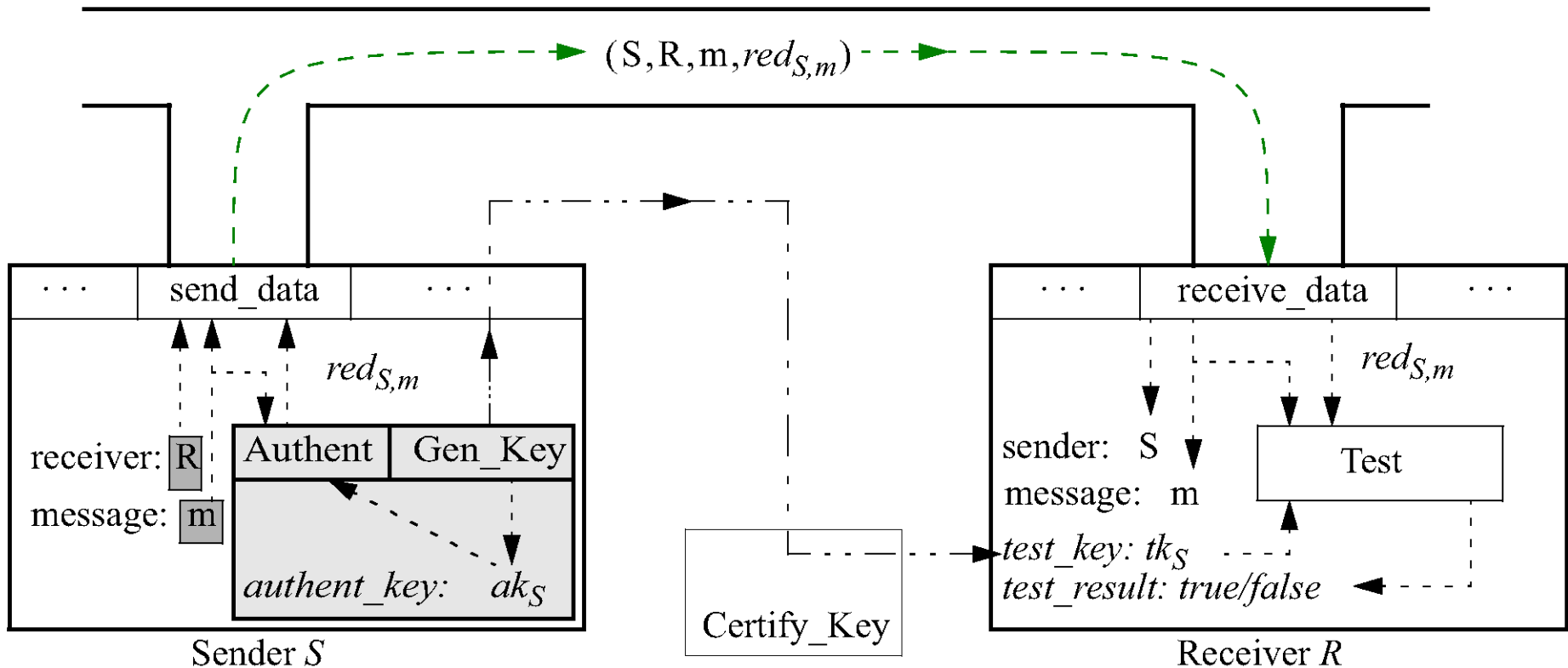


- ***symmetric (or secret-key) mechanism:***
  - the test key is (basically) *equal* to the authentication key
- ***asymmetric (or public-key) mechanism:***
  - the test key is essentially *different* from the authentication key
  - an additional *secrecy property (naive version)* is required:  
the (private) authentication key  $ak_S$   
cannot be “determined” from the (public) test key  $tk_S$

# Symmetric authentication



# Asymmetric authentication (digital signing)



# Symmetric and asymmetric authentication mechanisms



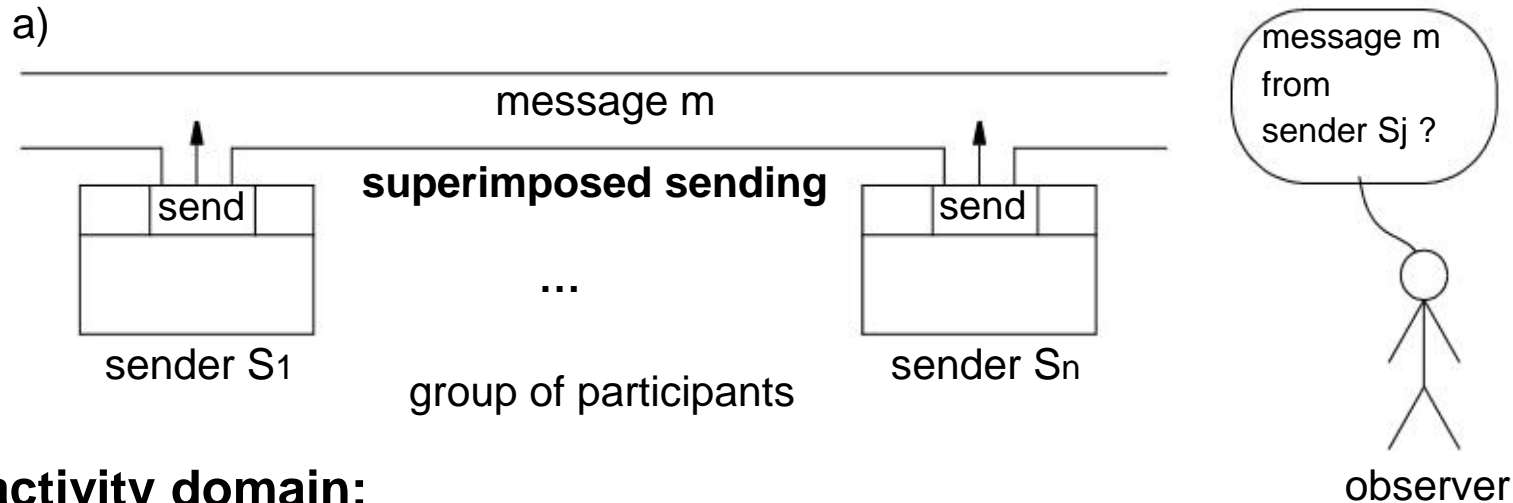
Feature	Symmetric	Asymmetric
generating and distributing keys	both partners are equally involved	designated sender has a distinguished role
protection requirements	key generation/ communication of the secret key and storage of the secret key must be protected on both sides	key generation  and storage of the private key must be protected on the side of the sender only
contributions of the trusted third parties	generate and distribute secret keys	certify public keys
non-repudiation/ digital signatures	no	yes



- the interest in *anonymity* or, more generally, in *non-observability* can be seen as strengthened forms of (message) *confidentiality*:
  - not only the message itself should be kept secret
  - but also the full *activity* of a message transmission
- from the point of view of an observer who is not designated to learn about an activity or a sequence of activities:
  - any actually occurring activity
  - is *indistinguishable* from
  - any other activity in a preferably large activity domain
  - from which the actually occurring activity has been selected
- the actual activity is *indistinguishably hidden* in a preferably large domain of other possibilities, often called an *anonymity class*

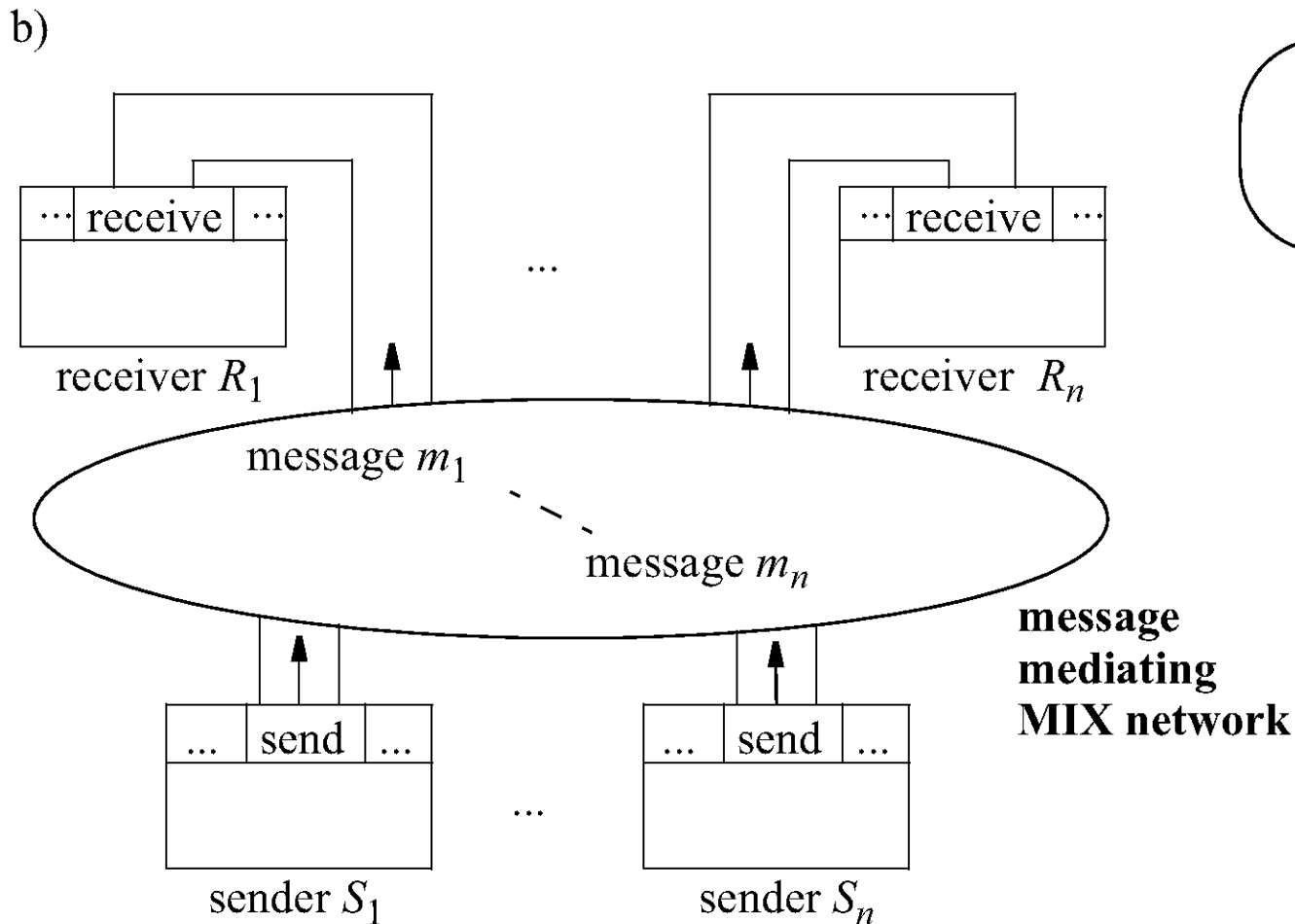


# Sender anonymity

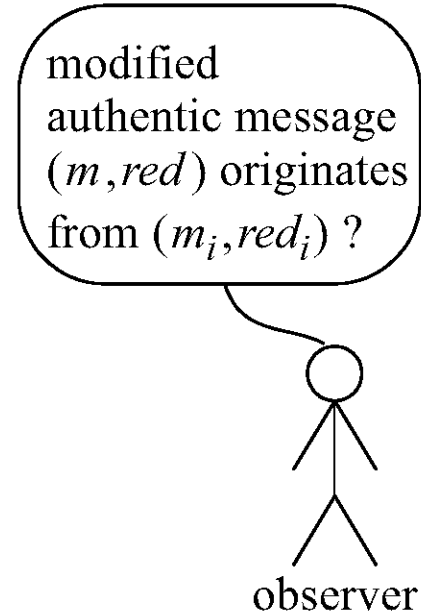
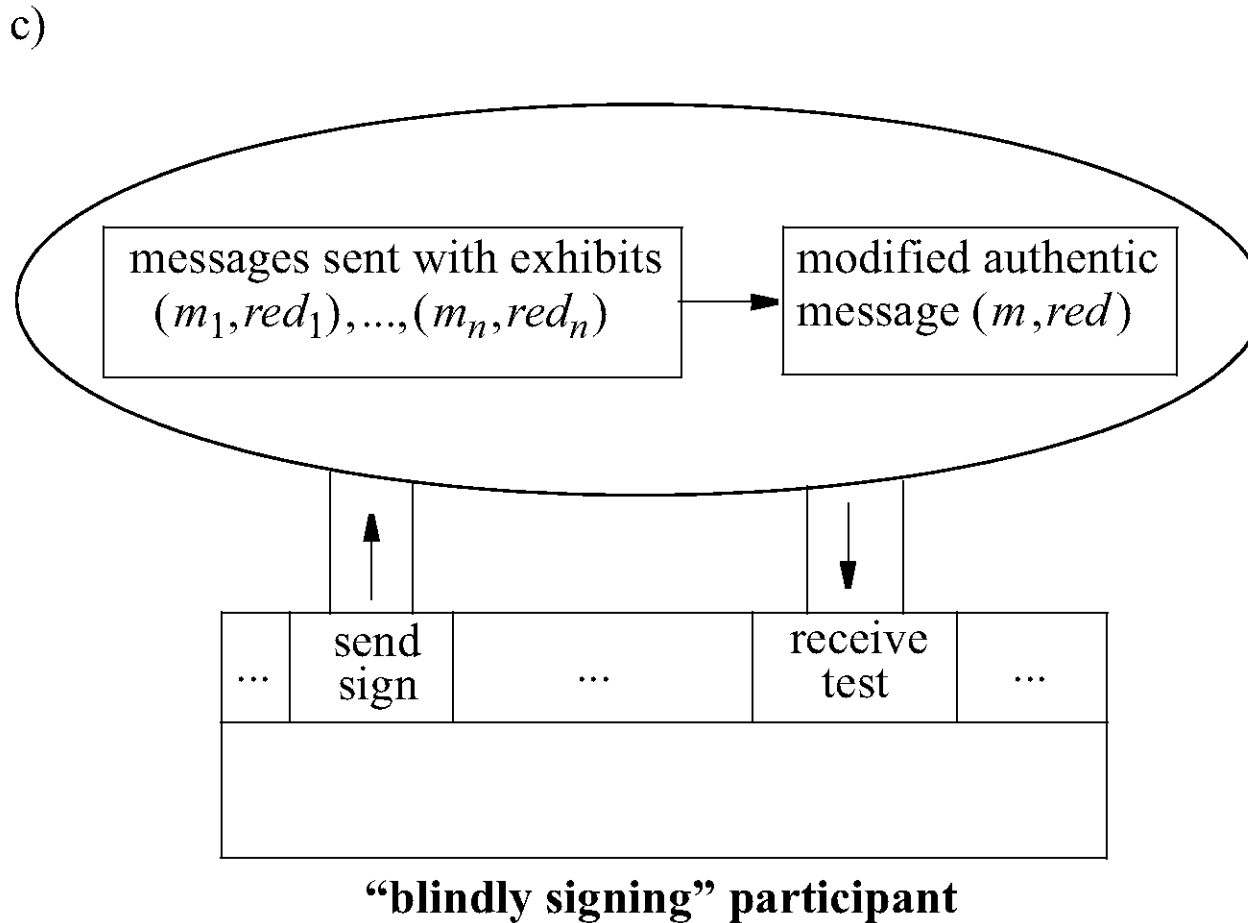


- **activity domain:**  
participants  $S_1, \dots, S_n$  sending and receiving messages
- **anonymity property:**  
by observing an actual message  $m$ ,  
a non-designated observer cannot “determine” the actual sender  $S_j$
- **mechanism:**  
*superimposed sending*

# Sender-receiver anonymity



# Anonymity by unlinkability



- **activity domain:**

- one distinguished participant *issues* (sends) digital documents (digitally signed messages) expressing some *obligation* to receivers
- receivers/holders *present* digital documents as a *credential (digital legitimation)* to be redeemed to the distinguished participant

- ***unlinkability property:***

knowing the issued documents  $\{(m_1, red_1), \dots, (m_n, red_n)\}$  and seeing a presented modified document  $(m, red)$  with a verified signature  $red$ , a non-designated observer cannot “determine” the link from the presented document to the corresponding issued document

- **mechanism:**

*blind signatures*

# A classification of pseudonyms



- regarding the *dissemination of knowledge* about the relationship between the pseudonym and the substituted subject, a pseudonym can be seen as
  - *public* (e.g., a phone number of an employee)
  - *confidential* (e.g., a bank account of a citizen)
  - *secret* (also called an *anonym*)
- regarding the intended *potentials for multiple use* and the resulting linkability, there are
  - *subject pseudonyms* for a broad range of activities
  - *role pseudonyms* for specific activities
  - *relationship pseudonyms* for activities addressing specific partners
  - combined *role-relationship pseudonyms* for specific activities addressing specific partners
  - *transaction pseudonyms (event pseudonyms)* for *single use only*

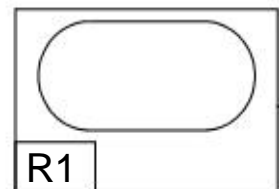
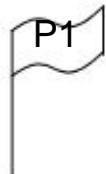
# Meanings of the notion of “participant” and their relationships



human individuals

pseudonyms

computing devices



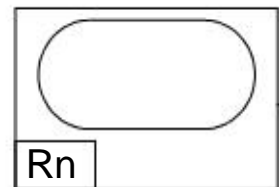
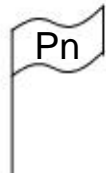
IP1

⋮

⋮

←→  
– possibly determined by application  
– might be inferrable from public knowledge

←→  
– application-oriented or action- (event-) oriented



IPn

network



- to achieve the indistinguishability goals of *cryptographic mechanisms*, *sufficient randomness* is needed
- a cryptographic mechanism *superimposes* the randomness of a secretly selected key, and possibly further inputs, on the returned items of interest such that the output items (ciphertexts, exhibits,...) again appear to be randomly taken
- making “sufficient randomness” algorithmically available is an outstanding open problem in computer science
- in fact, precisely defining the notion of “sufficient randomness” has already turned out to be a great challenge that has raised various proposals for an answer



- is a deterministic polynomial-time algorithm
- stretches a seed, a short and supposedly random input, into a much larger output sequence appearing again to be “sufficiently random”
- delivers outputs that should be *computationally indistinguishable* from a family of (ideal) uniformly distributed sequences:
  - there is no probabilistic polynomial-time algorithm that can distinguish the algorithmic outputs from the abstract ideal sequences with a non-negligible probability without knowing the seeds



# Guidelines for generating and employing pseudorandom sequences

- use some *physical source* for supplying (supposedly) “truly random” seeds of short length
- use a *pseudorandom generator* for stretching a supposedly random input seed into a much larger output sequence appearing again to be “sufficiently random”
- design a cryptographic mechanism (for encryption, authentication, etc.)
  - to take a “truly random” input
  - to superimpose the randomness of this input on the returned items (to be proven to comply with pertinent indistinguishability as well)
- for an actual *implementation*, however, replace the (ideal) “truly random” input by an actually available pseudorandom sequence
- verify a compositionality property of the *indistinguishability properties*, to ensure that the replacement does not affect the quality of the returned items

- to *generate* a *secret key* for some cryptographic mechanism:  
to designate its holder(s) as distinguished from all other participants
- to employ a random input as a *nonce*:  
to mark a message within some cryptographic protocol as unique and personal
- to *pad* a value from some (too small) domain with a random input:  
to define a modified domain sufficiently large to prevent successful guessing
- to *blind* some data with a random input using a reversible algebraic operation:  
to present that data to somebody else without revealing the actual value
- most generally, to *randomize* some algorithm of a cryptographic mechanism:  
to achieve a wanted indistinguishability property

# One-way hash functions



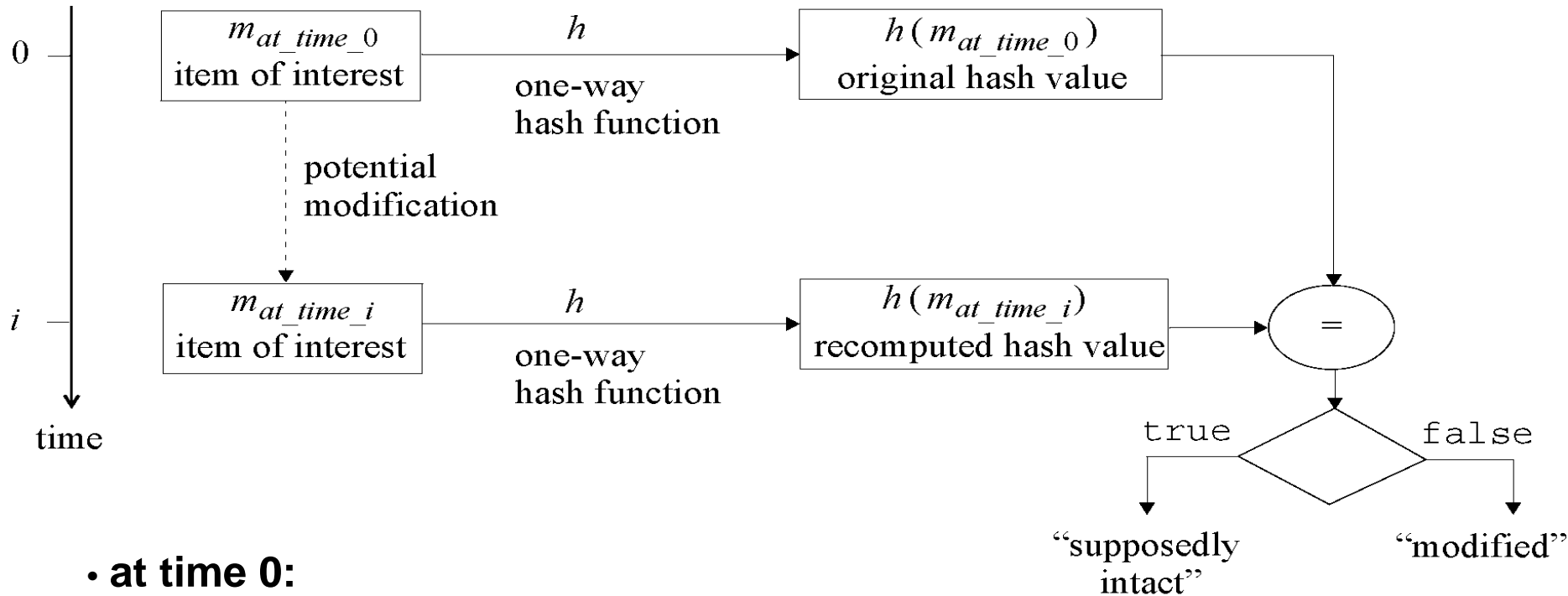
- some item of interest is often represented in a concise, disguised and unforgeable form, called a *fingerprint*, a *digest* or a *hash value*
- *concise*:
  - representation consists of a suitably short bit string of an agreed format
  - a large domain of items is mapped onto a small domain of representations: there must be collisions
- *disguised*:
  - a represented item cannot be “determined” from its representation
- *unforgeable*:
  - nobody can “determine” a representation of an item without a knowledge of that item
- *collision resistant*:
  - nobody can “determine” pairs of items that share a representation

# Application: representations with fixed short format



- a cryptographic protocol might demand an argument complying with a fixed short format for further processing, but the items of interest might vary or even be of arbitrary length
- example:  
some authentication protocols digitally sign the representations instead of the represented items

# Application: enforcing integrity (detection of modification)



- **at time 0:**
  - map the item onto its representation (original hash value)
  - store the item and its representation in different locations
- **at a later time  $i$ :**
  - compare the retrieved representation (original hash value) with a recomputed representation of the retrieved item (recomputed hash value)

# One-way hash functions: functionality and properties



- function  $h$  maps any element  $m$  of a (large) domain  $D$  (might be infinite) onto a bit string of a (short) fixed length  $l$ , i.e., onto an element of  $\{0,1\}^l$
- an assigned value  $h(m)$  is called the *hash value* of  $m$
- the function  $h$  must be efficiently computable, i.e., there is an efficient algorithm  $H$  that computes  $h(m)$  on input of  $m$
- the *inversion* of  $h$  must be computationally infeasible, i.e., the following roughly circumscribed *one-way property* is required:  
for all values  $z \in \{0,1\}^l$ ,  
one cannot “determine” a domain element  $m \in D$  such that  $h(m) = z$
- regarding the inevitable collisions (for large domain and short length), the function  $h$  must be *collision-resistant*

- should protect against a fraud  
where a given message  $m$  is exchanged for another one:
- for all domain elements  $m \in D$ ,  
one cannot “determine” a different domain element  $m' \in D$   
such that  $h(m) = h(m')$

# Strong collision-resistance property



- should totally block any attempt at a fraudulent exchange
- one cannot “determine”  
two different domain elements  $m \in D$  and  $m' \in D$   
such that  $h(m) = h(m')$
- equivalent to requiring  
that one cannot “determine”  
an element  $m \in D$   
that violates the weak version





- sometimes, *integrity as temporal correctness* should be supported
- in a proof of authenticity, the receiver should be able to evaluate
  - not only *who* has formed and sent a message
  - but also *when* these two events happened
- to prevent replay attacks or to achieve related goals, before authenticating a message, the sender can include a current *timestamp*
- considering the time span between
  - when the message was *formed* and
  - when it was *received*,the receiver can decide whether he is willing to accept the message as authentic or not
- all participants involved must share *synchronized clocks*;  
the receiver should take tolerable discrepancies in local times into account



- combined *temporal correctness and unforgeability property* is desired:  
for all messages  $m$  with an included timestamp  $ts$   
and suitably authenticated by the sender,  
from the perspective of a receiver,  
the actual *forming time* of the message  
coincides with the included *timestamp*
- participants might prefer to employ weaker  
but more readily manageable means than timestamps
- if only *relative* forming times are important,  
the sender might include *serial numbers* (instead of timestamps)
- a receiver not willing to rely on synchronized clocks might  
ask a sender to follow a *challenge-response procedure*  
in order to obtain evidence for the freshness of a received message



- cryptography aims at enabling participants to autonomously enforce their security interests even in the presence of threats
- a *threat* is instantiated by somebody/something performing a specific *attack*
- attack in theoretical investigations:  
an execution of a polynomially time-bounded probabilistic Turing machine
- attack in more practical investigations:  
exploiting a concrete attacking strategy
- *security requirements*:  
to be specified in terms of attacks
- *evaluating* a cryptographic mechanism:  
includes an analysis of the mechanism's robustness against attacks
- *classification framework* for attacks (on encryption mechanisms):  
here, from the point of view of attackers, describing their options for success

# A classification framework for attacks against encryption



- **kind of success**

- *exact*: exact new knowledge
- *probability-theoretic*: improved probability distribution

- **extent of success**

- *universal*: functional equivalence with decryption algorithm
- *complete*: gain of secret key
- *message-selective*: plaintexts of selected ciphertexts
- *message-existential*: plaintext of some ciphertext

- **target of attack**

- affect *human individuals*
- exploit *computing system*
- affect individuals and the system in *coordination*

# A classification framework for attacks against encryption



- **time of attack/attacked part**
  - subvert *overall system*
  - subvert *key generation*
  - subvert *key distribution*
  - exploit *message transmissions*
- **method of attack (against message transmissions)**
  - *passive*: observe messages [ciphertext/plaintext pairs]
  - *active*: observe plaintexts [ciphertexts] of chosen ciphertexts [plaintexts]
- **planning of active attack**
  - *non-adaptive*: choose statically at the beginning
  - *adaptive*: choose dynamically depending on progress
- **expectation of success**
  - *probability-theoretic*: upper bound for success probability
  - *complexity-theoretic*: lower bound for needed resources
  - *combined*: upper bound for success probability with limited resources



- a participant designated to hold some secret or private keys must be able to secretly generate, store and use these keys; best if the participant controls a *personal tamper-resistant computing device*
- secret and private keys and possibly further items have to appear as random, and, accordingly, some *source of randomness* should be available; best possibility being a *truly random* physical source
- items to appear as random must have *sufficient length* to resist attacks based on *exhaustive search and trials*
- some assistance of a *trusted third party* is normally required
- various further *external participants* contribute to an application of a cryptographic mechanism; assigning *trust* to them should be based on *open design* and *informational assurances*